# Cryptography and Network Security Chapter 3 

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## Modern Block Ciphers

> now look at modern block ciphers
$>$ one of the most widely used types of cryptographic algorithms
$>$ provide secrecy /authentication services
$>$ focus on DES (Data Encryption Standard)
> to illustrate block cipher design principles

## Block vs Stream Ciphers

ylock ciphers process messages in blocks, each of which is then en/decrypted
$>$ like a substitution on very big characters - 64-bits or more
> stream ciphers process messages a bit or byte at a time when en/decrypting
> many current ciphers are block ciphers
$>$ broader range of applications

## Illustration of Block Cipher Technique



## Block vs Stream Ciphers



## Block vs Stream Ciphers



## Block Cipher Principles

most symmetric block ciphers are based on a Feistel Cipher Structure
> block ciphers look like an extremely large substitution
> In general, for an n-bit ideal block cipher, the length of the key defined in this fashion is $n \times 2^{n}$ bits.

## Ideal Block Cipher



## Claude Shannon and SubstitutionPermutation Ciphers

> Claude Shannon introduced idea of substitutionpermutation (S-P) networks in 1949 paper
$>$ form basis of modern block ciphers
> S-P nets are based on the two primitive cryptographic operations seen before:

- substitution (S-box)
- permutation (P-box)
> provide confusion \& diffusion of message \& key


## Confusion and Diffusion

> cipher needs to completely obscure statistical properties of original message
> a one-time pad does this
$>$ more practically Shannon suggested combining S \& P elements to obtain:
$>$ diffusion - dissipates statistical structure of plaintext over bulk of ciphertext
> confusion - makes relationship between ciphertext and key as complex as possible

## Feistel Cipher Structure

partitions input block into two halves

- process through multiple rounds which
- perform a substitution on left data half
- based on round function of right half \& subkey
- then have permutation swapping halves
> implements Shannon's S-P net concept


## Feistel Cipher Structure



## Feistel Cipher Design Elements

> block size
$>$ key size
$>$ number of rounds
$>$ subkey generation algorithm
$>$ round function
> fast software en/decryption
> ease of analysis

## Feistel Cipher Decryption



## Data Encryption Standard (DES)

$>$ most widely used block cipher in world
> adopted in 1977 by NBS (now NIST)

- as FIPS PUB 46
$>$ encrypts 64-bit data using 56-bit key
> has widespread use


## DES History

> IBM developed Lucifer cipher

- by team led by Feistel in late 60's
- used 64-bit data blocks with 128-bit key
$>$ then redeveloped as a commercial cipher with input from NSA and others
> in 1973 NBS issued request for proposals for a national cipher standard
>IBM submitted their revised Lucifer which was eventually accepted as the DES


## DES Encryption Overview



## Initial Permutation IP

$>$ first step of the data computation
> IP reorders the input data bits
> even bits to LH half, odd bits to RH half
> quite regular in structure (easy in $\mathrm{h} / \mathrm{w}$ )
> example:

$$
\begin{gathered}
\operatorname{IP}(675 a 6967 \text { 5e5a6b5a) }= \\
(-------004 d f 6 f b)
\end{gathered}
$$

## Initial Permutation (IP)

| 58 | 50 | 42 | 34 | 26 | 18 | 10 | 2 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 60 | 52 | 44 | 36 | 28 | 20 | 12 | 4 |
| 62 | 54 | 46 | 38 | 30 | 22 | 14 | 6 |
| 64 | 56 | 48 | 40 | 32 | 24 | 16 | 8 |
| 57 | 49 | 41 | 33 | 25 | 17 | 9 | 1 |
| 59 | 51 | 43 | 35 | 27 | 19 | 11 | 3 |
| 61 | 53 | 45 | 37 | 29 | 21 | 13 | 5 |
| 63 | 55 | 47 | 39 | 31 | 23 | 15 | 7 |

## Initial Permutation IP

$>$ first step of the data computation
$>$ IP reorders the input data bits
> even bits to LH half, odd bits to RH half
> quite regular in structure (easy in $\mathrm{h} / \mathrm{w}$ )
> example:

```
IP(675a6967 5e5a6b5a) = (ffb2194d
004df6fb)
```


## DES Round Structure

> uses two 32-bit L \& R halves
> as for any Feistel cipher can describe as:

$$
\begin{aligned}
& L_{i}=R_{i-1} \\
& R_{i}=L_{i-1} \oplus \mathrm{~F}\left(R_{i-1}, K_{i}\right)
\end{aligned}
$$

$>F$ takes 32-bit $R$ half and 48-bit subkey:

- expands R to 48-bits using perm E
- adds to subkey using XOR
- passes through 8 S-boxes to get 32-bit result
- finally permutes using 32-bit perm P


## Single Round of DES Algorithm



## Calculation of $\mathrm{F}(\mathrm{R}, \mathrm{K})$



## The Expansion Permutation E

|  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: |
| 32 | 1 | 2 | 3 | 4 | 5 |
| 4 | 5 | 6 | 7 | 8 | 9 |
| 8 | 9 | 10 | 11 | 12 | 13 |
| 12 | 13 | 14 | 15 | 16 | 17 |
| 16 | 17 | 18 | 19 | 20 | 21 |
| 20 | 21 | 22 | 23 | 24 | 25 |
| 24 | 25 | 26 | 27 | 28 | 29 |
| 28 | 29 | 30 | 31 | 32 | 1 |

## DES Expansion Permutation



> R half expanded to same length as 48-bit subkey
> consider R as 8 nybbles (4 bits each)
> expansion permutation

- copies each nybble into the middle of a 6-bit block
- copies the end bits of the two adjacent nybbles into the two end bits of the 6-bit block


## Calculation of $\mathrm{F}(\mathrm{R}, \mathrm{K})$



## Substitution Boxes S

> have eight S-boxes which map 6 to 4 bits
> each S-box is actually 4 little 4 bit boxes

- outer bits 1 \& 6 (row bits) select one row of 4
- inner bits 2-5 (col bits) are substituted
- result is 8 lots of 4 bits, or 32 bits
> row selection depends on both data \& key
- feature known as autoclaving (autokeying)

Box $\mathrm{S}_{1}$

| 0 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 14 | 4 | 13 | 1 | 2 | 15 | 11 | 8 | 3 | 10 | 6 | 12 | 5 | 9 | 0 | 7 |
| 1 | 0 | 15 | 7 | 4 | 14 | 2 | 13 | 1 | 10 | 6 | 12 | 11 | 6 | 5 | 3 | 8 |
|  | 4 | 1 | 14 | 8 | 13 | 6 | 2 | 11 | 15 | 12 | 9 | 7 | 3 | 10 | 5 | 0 |
|  | 15 | 12 | 8 | 2 | 4 | 9 | 1 | 7 | 5 | 11 | 3 | 14 | 10 | 0 | 6 | 13 |

For example, $\mathrm{S}_{1}(101010)=6=0110$.

## Calculation of $\mathrm{F}(\mathrm{R}, \mathrm{K})$



## Permutation Function (P)

(d) Permutation Function (P)

| 16 | 7 | 20 | 21 | 29 | 12 | 28 | 17 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 15 | 23 | 26 | 5 | 18 | 31 | 10 |
| 2 | 8 | 24 | 14 | 32 | 27 | 3 | 9 |
| 19 | 13 | 30 | 6 | 22 | 11 | 4 | 25 |

## Single Round of DES Algorithm



## DES Key Schedule

$>$ forms subkeys used in each round

- initial permutation of the key (PC1) which selects 56 -bits in two 28 -bit halves
- 16 stages consisting of:
- rotating each half separately either 1 or 2 places depending on the key rotation schedule K
- selecting 24-bits from each half \& permuting them by PC2 for use in round function F
> note practical use issues in h/w vs s/w


## Permuted Choice One (PC1)

| 57 | 49 | 41 | 33 | 25 | 17 | 9 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 58 | 50 | 42 | 34 | 26 | 18 |
| 10 | 2 | 59 | 51 | 43 | 35 | 27 |
| 19 | 11 | 3 | 60 | 52 | 44 | 36 |
| 63 | 55 | 47 | 39 | 31 | 23 | 15 |
| 7 | 62 | 54 | 46 | 38 | 30 | 22 |
| 14 | 6 | 61 | 53 | 45 | 37 | 29 |
| 21 | 13 | 5 | 28 | 20 | 12 | 4 |

## Schedule of Left Shifts

| Round Number | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Bits Rotated | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 1 |

## Permuted Choice Two (PC-2)

| 14 | 17 | 11 | 24 | 1 | 5 | 3 | 28 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 15 | 6 | 21 | 10 | 23 | 19 | 12 | 4 |
| 26 | 8 | 16 | 7 | 27 | 20 | 13 | 2 |
| 41 | 52 | 31 | 37 | 47 | 55 | 30 | 40 |
| 51 | 45 | 33 | 48 | 44 | 49 | 39 | 56 |
| 34 | 53 | 46 | 42 | 50 | 36 | 29 | 32 |

## DES Round in Full






 Right Haffi


## DES Decryption

> decrypt must unwind steps of data computation
> with Feistel design, do encryption steps again using subkeys in reverse order (SK16 ... SK1)

- IP undoes final FP step of encryption
- 1st round with SK16 undoes 16th encrypt round
- 16th round with SK1 undoes 1 st encrypt round
- then final FP undoes initial encryption IP
- thus recovering original data value


## DES Decryption



## Avalanche Effect

$>$ key desirable property of encryption alg
$>$ where a change of one input or key bit results in changing approx half output bits
$>$ making attempts to "home-in" by guessing keys impossible
> DES exhibits strong avalanche

## Avalanche Effect

| Round |  | $\delta$ | Round |  | $\delta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 02468 aceeca86420 <br> 12468 aceeca86420 | 1 | 9 | c11bfc09887fbc6c 99f911532eed7d94 | 32 |
| 1 | 3cf03c0fbad22845 <br> 3cf03c0fbad32845 | 1 | 10 | 887 fbc 6 c 600 f 7 e 8 b 2eed7d94d0f23094 | 34 |
| 2 | bad2284599e9b723 <br> bad3284539a9b7a3 | 5 | 11 | 600f7e8bf596506e d0f23094455da9c4 | 37 |
| 3 | 99e9b7230bae3b9e <br> 39a9b7a3171cb8b3 | 18 | 12 | f596506e738538b8 <br> 455da9c47f6e3cf3 | 31 |
| 4 | Obae3b9e42415649 <br> 171 cb 8 b 3 ccaca 55 e | 34 | 13 | 738538 b 8 c 6 a 62 c 4 e <br> $7 f 6 e 3 c f 34 b c 1 a 8 d 9$ | 29 |
| 5 | 4241564918b3fa41 ccaca55ed16c3653 | 37 | 14 | c6a62c4e56b0bd75 4 bc 1 a 8 d 91 e 07 d 409 | 33 |
| 6 | 18b3fa419616fe23 <br> d16c3653cf402c68 | 33 | 15 | 56b0bd7575e8fd8f <br> 1e07d4091ce2e6dc | 31 |
| 7 | 9616fe2367117cf2 <br> cf 402 c 682 b 2 cefbc | 32 | 16 | 75 e 8 fd 8 f 25896490 <br> 1ce2e6dc365e5f59 | 32 |
| 8 | 67117 cf 2 c 11 bfc 09 <br> 2b2cefbc99f91153 | 33 | $\mathrm{IP}^{-1}$ | da02ce3a89ecac3b 057cde97d7683f2a | 32 |

## Strength of DES - Key Size

$>56$-bit keys have $2^{56}=7.2 \times 10^{16}$ values
$>$ brute force search looks hard
> recent advances have shown is possible

- in 1997 on Internet in a few months
- in 1998 on dedicated h/w (EFF) in a few days
- in 1999 above combined in 22hrs!
$>$ still must be able to recognize plaintext
must now consider alternatives to DES


## Block Cipher Design

basic principles still like Feistel's in 1970's
$>$ number of rounds

- more is better, exhaustive search best attack
$>$ function f :
- provides "confusion", is nonlinear, avalanche
- have issues of how S-boxes are selected
>key schedule
- complex subkey creation, key avalanche


## Summary

> have considered:

- block vs stream ciphers
- Feistel cipher design \& structure
- DES
- details
- strength
- block cipher design principles

